



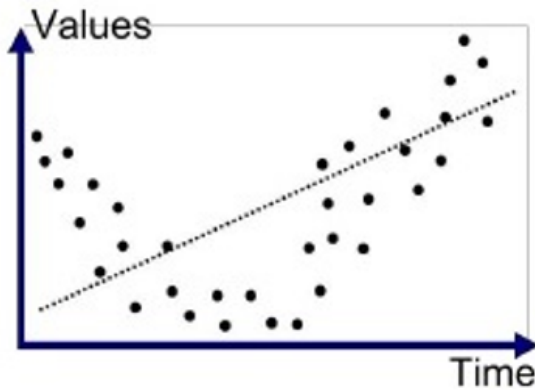
# Basics

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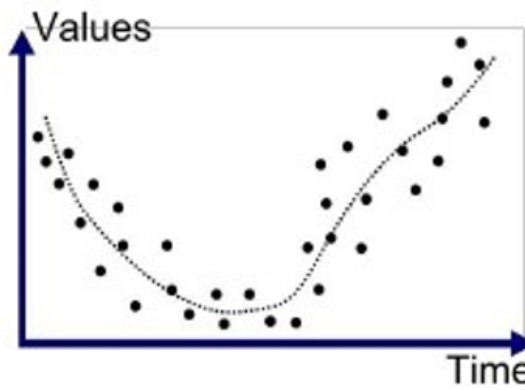
## Independent and identically distributed random variables

- a collection of random variables is **independent and identically distributed** if each random variable has the same probability distribution as the others and all are mutually independent.
- Examples of i.i.d. : Sample with replacement (the result of the n-th draw)
- Independent, non-identical distribution: the lottery changes its content after each draw
- Dependent, non-identically-distributed : temporal correlation, the sample from the previous time step affects the outcome of next sample.
- E.g. sample without replacement (take a draw from lottery, but not putting the draw back.)

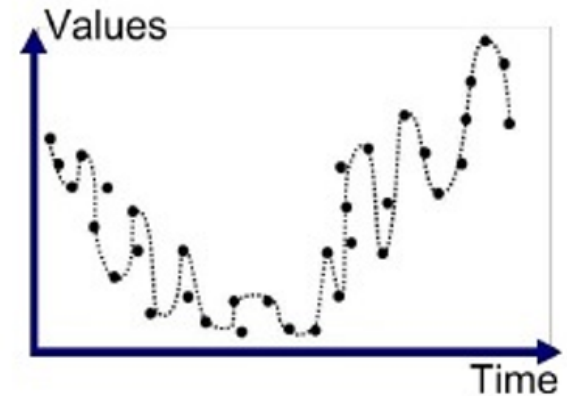
## Underfit v.s. Overfit



Underfitted



Good Fit/Robust



Overfitted

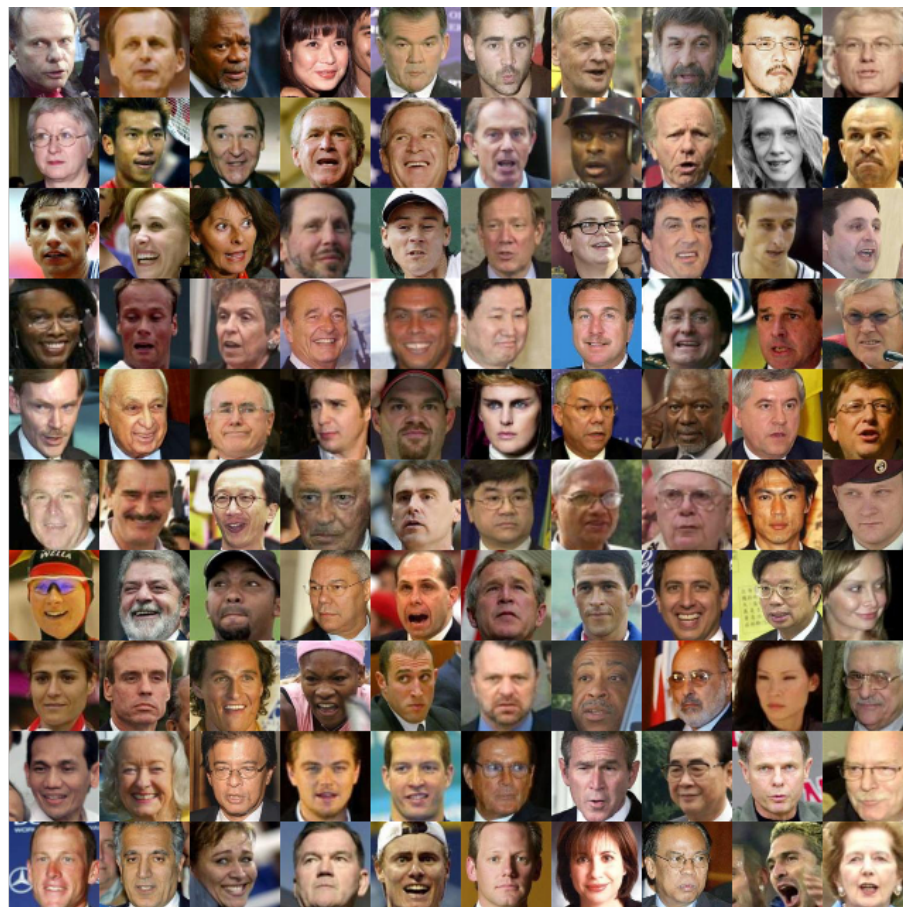
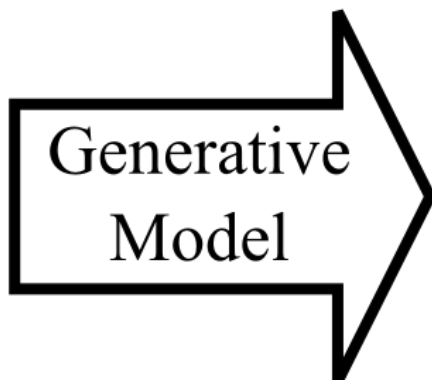
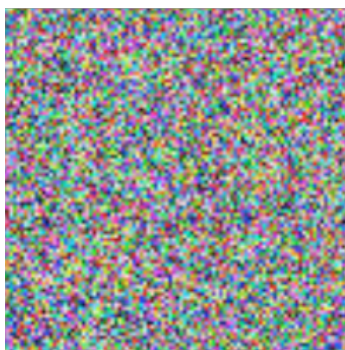
- The rule of Occam's Razor
  - Apply the simplest model which can explain the data → generalize well

## Generative model v.s. Discriminative model

- $X$  : data instances,  $Y$  : Labels
- **Generative models** capture the joint probability  $p(X, Y)$ , or just  $p(X)$  if there are no labels.
- E.g. Generative-Adversarial Networks , can generate new photos of animals that look like real animals
  
- **Discriminative models** discriminate between different kinds of data instances, ignores the question of whether a given instance is likely.
- Only captures the conditional probability  $p(Y | X)$
- E.g. Logistic regression, decision tree , can only tell a dog from a cat

# An illustration of GAN

Noise  $\sim N(0,1)$





# Data

- <https://github.com/NRottmann/Toolbox-GP-GMRF>